

Fortran coarray/MPI Multi-Scale CAFE for Fracture in Heterogeneous Materials

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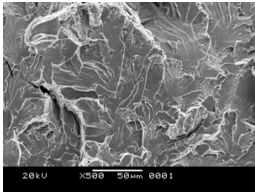
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Fracture in heterogeneous materials



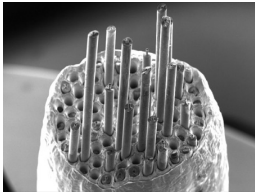
polycrystal cleavage



reinforced concrete



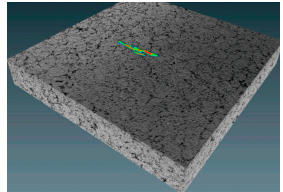
CFRP



metal matrix



bone

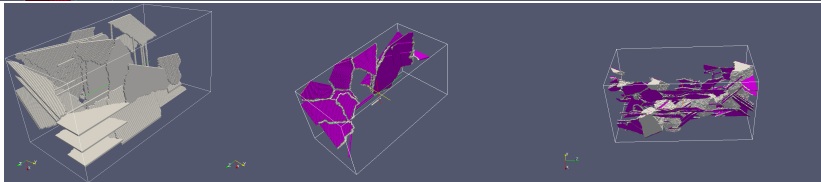
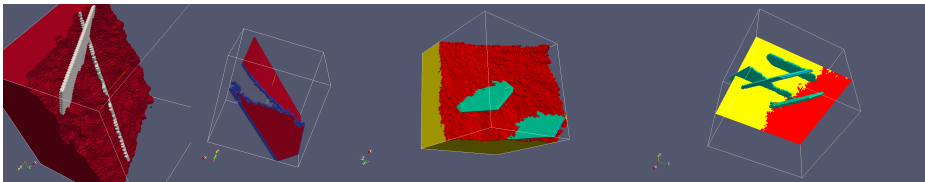


graphite

- ▶ All real materials are heterogeneous
- ▶ Multiple fracture and damage processes happen at different time and length scales → **need multi-scale framework**

Fracture: CA + FE = CAFE multi-scale model ▶ CGPACK

- ▶ **Structured grids** - cellular automata (CA), **unstructured grids** - finite elements (FE)
- ▶ CA (microstructure) + FE (continuum mechanics) = CAFE
- ▶ Transgranular cleavage - fracture stress or strain criteria
- ▶ FE \rightarrow CA (localisation) - stress, strain fields
- ▶ CA \rightarrow FE (homogenisation) - damage variables

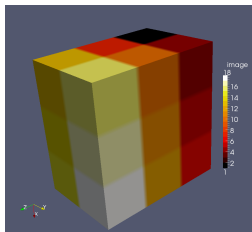


Fortran coarrays for CA

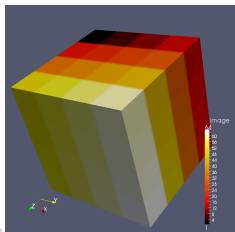
- ▶ Fortran native SPMD parallel programming feature
- ▶ Fortran standard since 2008. More features in 2015.
- ▶ Cray, Intel, OpenCoarrays/GCC support
- ▶ CGPACK - cellular automata microstructure simulation library: cgpack.sf.net. See also [1, 2, 3, 4].
- ▶ Easy halo exchange
- ▶ CA space coarray - 4D array, 3 codimensions:

```
integer, allocatable :: space (:, :, :, :)[ :, :, :, :]
```

- ▶ Ideal for **structured** grids:



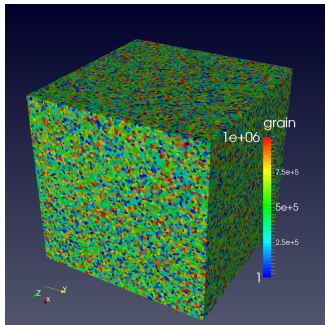
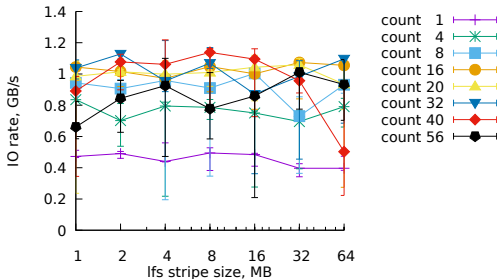
← 18 imgs; 64 imgs →



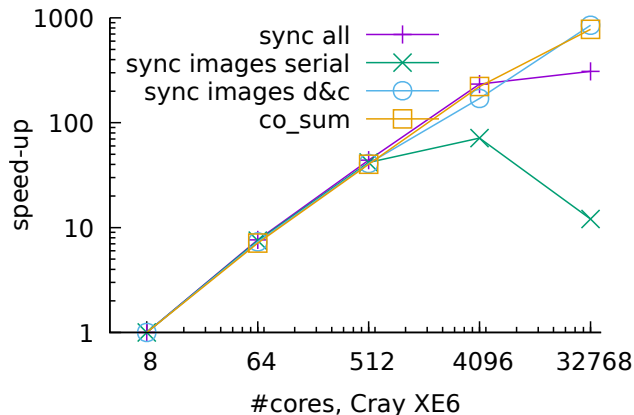
Coarray IO - no native Fortran parallel IO

- ▶ MPI/IO up to 2.3GB/s on Cray XE6 [▶ BCS talk](#)
- ▶ MPI/IO up to 8GB/s on Cray XC30 (can reach 14GB/s [5])
- ▶ NetCDF 4.3, HDF5 1.8.14 - only up to 1.2GB/s on Cray XC30.
- ▶ lfs stripe count, size, number of images, file size, Cray hugepages...
- ▶ 0.5 - 1TB datasets

Cray XC30, 20 nodes, lfs, NetCDF IO rates



CGPACK solidification scaling



Scaling varies for different programs built with CGPACK, depending on which routines are called, in what order and requirements for synchronisation.

ParaFEM - scalable general purpose finite element library

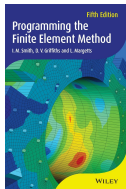
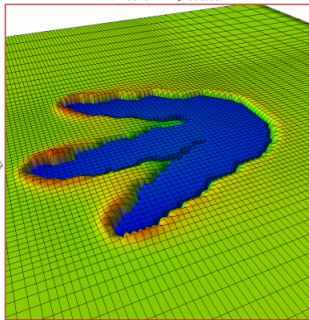
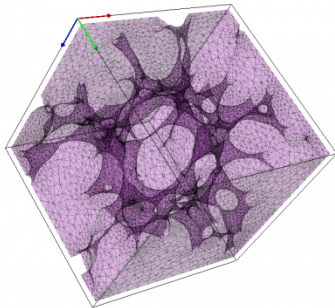
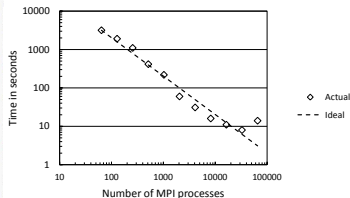
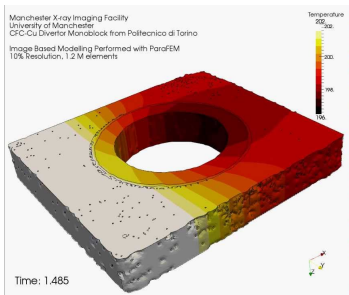
▶ <http://parafem.org.uk>

▶ Fortran 90
MPI

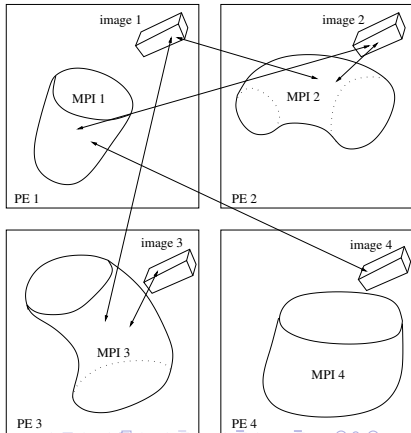
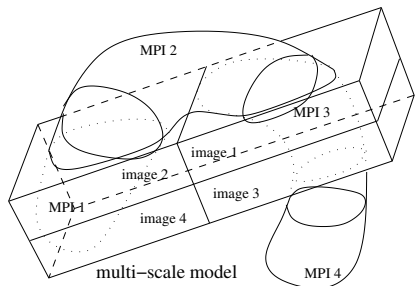
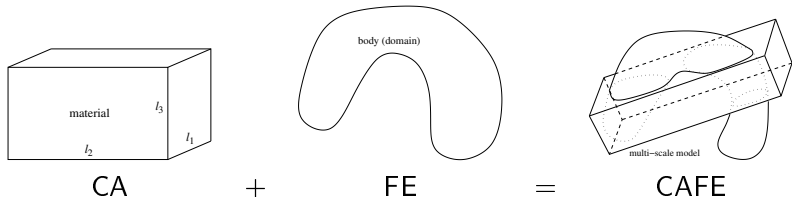
▶ Highly portable,
many users
[6]

▶ Excellent
scaling

▶ BSD license

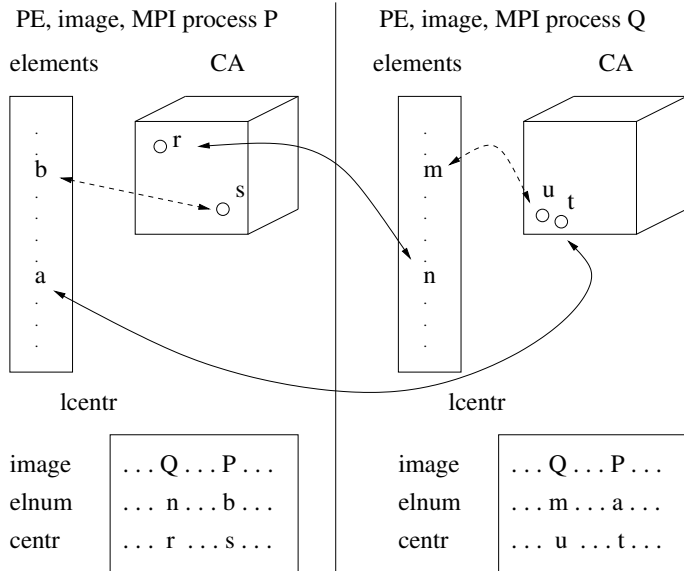


CAFE design: structured CA grid + unstructured FE grid



Example with 4 PE (4 MPI processes, 4 coarray images). Arrows are FE \leftrightarrow CA comms.

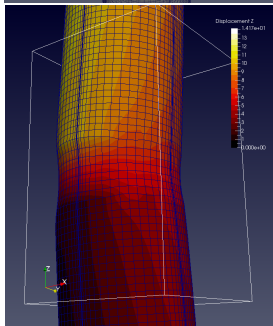
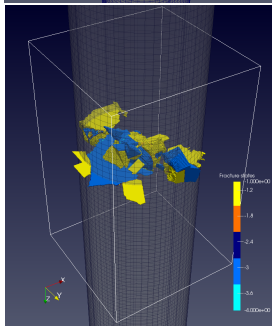
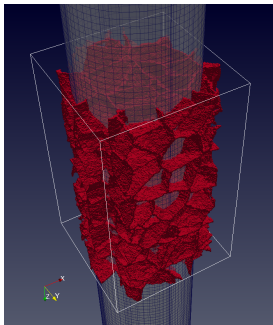
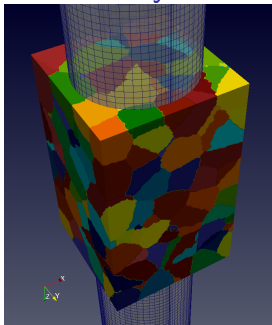
lcentr arrays on images P and Q



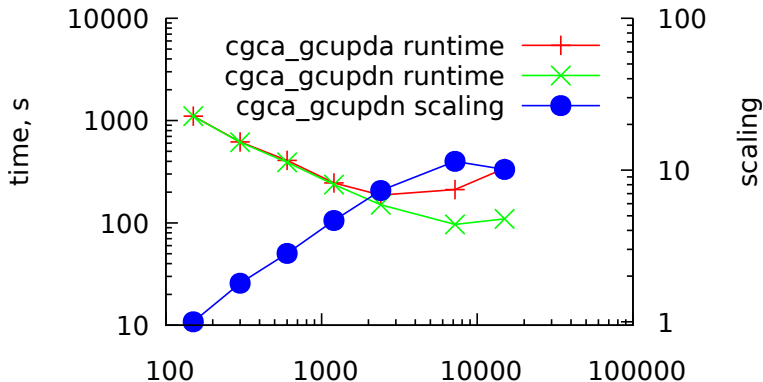
Fracture modelling

- ▶ Diverse CAFE fracture models can be constructed from CGPACK + ParaFEM libraries.
- ▶ Simple case: isotropic linear elastic FE (E, ν) + cleavage (fully brittle transgranular fracture mode) CA.
- ▶ FE stress tensor \mathbf{t} passed to CA, resolved on normal stresses on $\{100\}$ and $\{110\}$ crystal planes - t_{100}, t_{110} [2, 7].
- ▶ 2 parameters - fracture stress, σ_F , linked to the free surface energy, γ , and a characteristic length, L .
- ▶ If $t_{100} \geq \sigma_F$ or $t_{110} \geq \sigma_F$ then a CA crack extends by L per unit of time.
- ▶ Crack morphology is reduced to a single damage variable, d . $d = 1$ initially (no damage). $d = 0$ - integration point has failed, no load bearing capacity.

Cleavage in a steel cylinder under tension



Scaling improvement with cgca_gcupdn over cgca_gcupda



Number of cores, ARCHER, Cray XC30

Runtimes and scaling for ParaFEM/CGPACK MPI/coarray miniapp with the nearest neighbour, cgca_gcupdn, and all-to-all, cgca_gcupda, algorithms.

Scaling limit increased from 2k to 7k cores.

CA - coarray (over)synchronisation?

```
call cgca_nr( space ) ! sync all inside
call cgca_rt( grt ) ! sync all inside
call cgca_sld( space ) ! sync all inside
call cgca_igb( space )
sync all
call cgca_hxi( space )
sync all
call cgca_gbs( space )
sync all
call cgca_hxi( space )
sync all
call cgca_gcu( space ) ! local routine no sync
```

- ▶ All images sync with their 26 neighbours.
- ▶ Some routines have sync inside.
- ▶ Other sync responsibility is left to end user.

Fortran 2015 events: more flexible than SYNC IMAGES [8]

```
use, intrinsic iso_fortran_env, only: event_type
type(event_type) :: var[:, :, :]
integer, allocatable :: space(:, :, :, :)[:, :, :]
integer :: errstat, myrank(3)
! allocate var, space
myrank = this_image( space )
! do some work, then notify neighbours
event post(                                     &
    var[ myrank(1)-1, myrank(2), myrank(3) ], &
    stat=errstat)
! 25 more posts
:
event wait(var, until_count=26, stat=errstat)
! when all 26 neighbours posted, continue work
:
```

Future: thread level parallelism: OpenMP, DO CONCURRENT

```
main: do iter = 1,N
  do x3 = lbr(3), ubr(3)
  do x2 = lbr(2), ubr(2)
  do x1 = lbr(1), ubr(1)
    live: if ...
      call cgca_clvgn( clvgflag )
      if ( clvgflag ) call sub( space )
    end if live
  end do
end do
end do
end do
call co_sum( clvgglob )
sync all
call cgca_hxi( space )
sync all
call cgca_dacf( space )
```

Conclusions

- ▶ Fortran coarrays are an ideal match for cellular automata
- ▶ Hybrid coarray+MPI multi-scale fracture framework is feasible
- ▶ Scaling up to 7k cores currently, work ongoing
- ▶ Profiling/tracing tools: CrayPAT, TAU, Score-P, Scalasca - coarray support is improving
- ▶ Coarray synchronisation - major issue: data integrity & performance

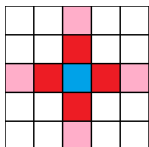
Acknowledgements

- ▶ This work was funded under the embedded CSE programme of the ARCHER UK National Supercomputing Service (<http://www.archer.ac.uk>), [archer.ac.uk](http://www.archer.ac.uk)
- ▶ This work was carried out using the computational facilities of the Advanced Computing Research Centre, University of Bristol - <https://www.acrc.bris.ac.uk>, www.acrc.bris.ac.uk

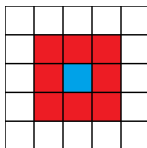
Cellular automata (CA) basics

- ▶ discrete space, discrete time, discrete states - fully digital framework, **structured grids**
- ▶ finite or infinite space
- ▶ finite space: fixed or self-similar boundaries

- ▶ cell neighbourhood, e.g. von Neumann's:



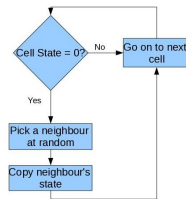
or Moore's:



- ▶ iterative process
- ▶ state of a cells at next iteration is a function of the state of this cells and of the states of its neighbourhood cells at the current iteration

Primitive 3D solidification - probabilistic CA

- ▶ States: liquid = 0, crystals > 0.
- ▶ Cell state uniquely encodes crystal orientation tensor, i.e. a look-up table.
- ▶ Each iteration a liquid cell acquires a state of a randomly chosen neighbour (3D Moore's neighbourhood - 26 cells).



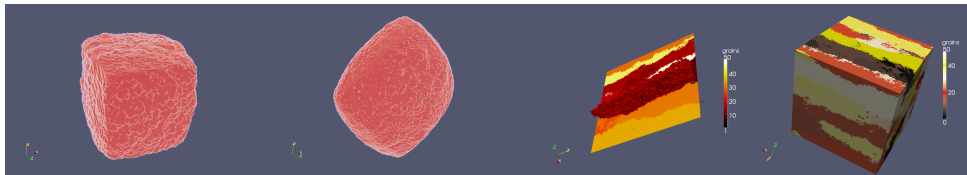
0	0	0	0	0	1	1	1	1
0	0	0	0	0	1	1	1	1
0	0	0	0	0	1	1	1	1
0	0	0	0	0	1	1	24	24
0	0	0	0	0	24	1	24	24
0	0	0	0	0	24	24	24	24
0	0	0	0	0	24	24	24	24
0	0	0	0	0	24	24	24	24
0	0	0	0	0	24	24	24	24
0	0	0	0	0	24	24	24	24

i

0	0	0	1	1	1	1	1	1
0	0	0	0	1	1	1	1	1
0	0	0	1	1	1	1	1	1
0	0	0	0	24	1	1	24	24
0	0	0	0	0	24	1	24	24
0	0	0	0	0	24	24	24	24
0	0	0	24	24	24	24	24	24
0	0	24	24	24	24	24	24	24
0	0	24	24	24	24	24	24	24

$i + 1$

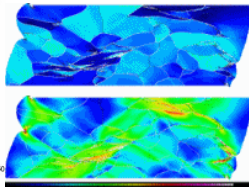
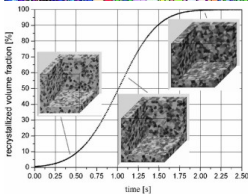
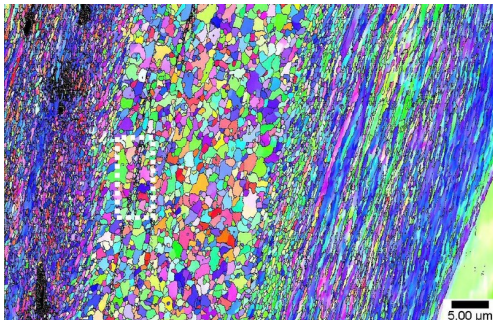
Primitive probabilistic 3D solidification - results



For more results [▶ CGPACK](#)

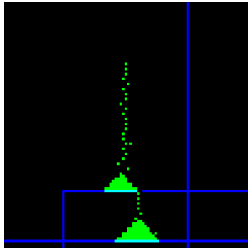
Recrystallisation

- ▶ The grain boundary velocity $\dot{\mathbf{x}} = \mathbf{n}mp$, \mathbf{n} - the normal to the grain boundary segment, m - mobility, p - the driving force.
- ▶ If $\dot{\mathbf{x}}\Delta t \geq c$, where Δt - time increment, c - cell size, then a cell joins the growing grain.
- ▶ Mobility strongly depends on temperature:
 $m \approx \alpha \exp(-\beta/T)$, α, β - some parameters, T - temperature.

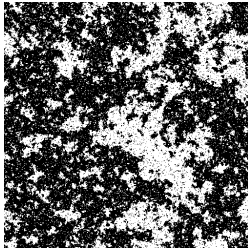


▶ Dierk Raabe site

Other CA examples



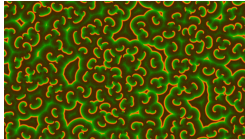
Sand pile formation



Ising magnetisation [▶ more info](#)



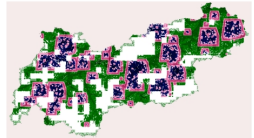
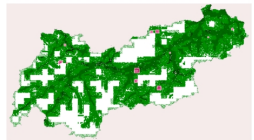
Land use [▶ more info](#)



Diffusion [▶ animation](#) [▶ info](#)



Fire [▶ more info](#)

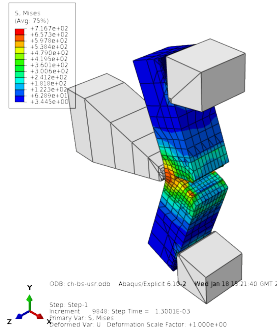
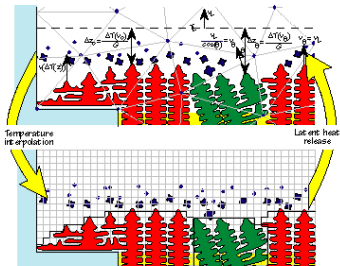
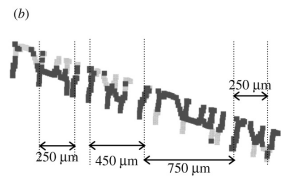
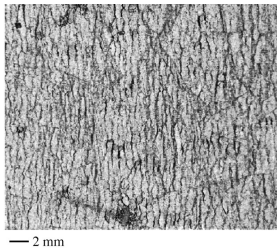


Epidemics, from *The Open Med. Inform. J.* 2(1):70-81, 2008.

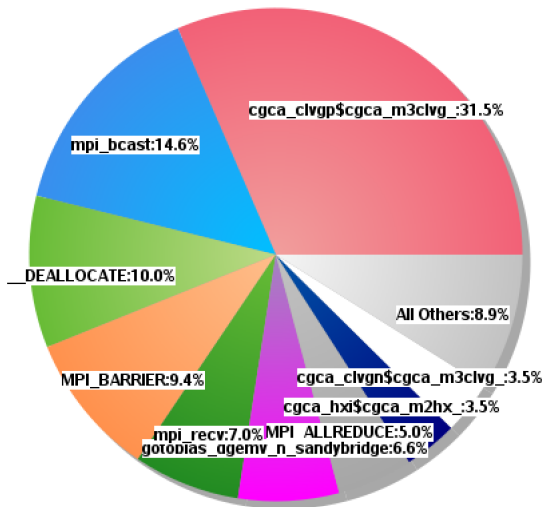
[▶ PDF](#)

More CAFE examples

- ▶ Used for solidification [9], recrystallisation [10] and fracture [11, 12].
- ▶ FE - continuum mechanics - stress, strain, etc.
- ▶ CA - crystals, crystal boundaries, cleavage, grain boundary fracture
- ▶ FE → CA - stress, strain
- ▶ CA → FE - damage variables



Profiling with cgca_pfem_map



Profiling function distribution for ParaFEM/CGPACK MPI/coarray miniapp with cgca_gcupdn and cgca_pfem_map at 7200 cores.

Profiling with cgca_pfem_map

Table 1: Profile by Function

Samp%	Samp	Imb. Samp	Imb. Samp%	Group	Function
100.0%	9,903.4	--	--	Total	

43.6%	4,321.6	--	--	USER	

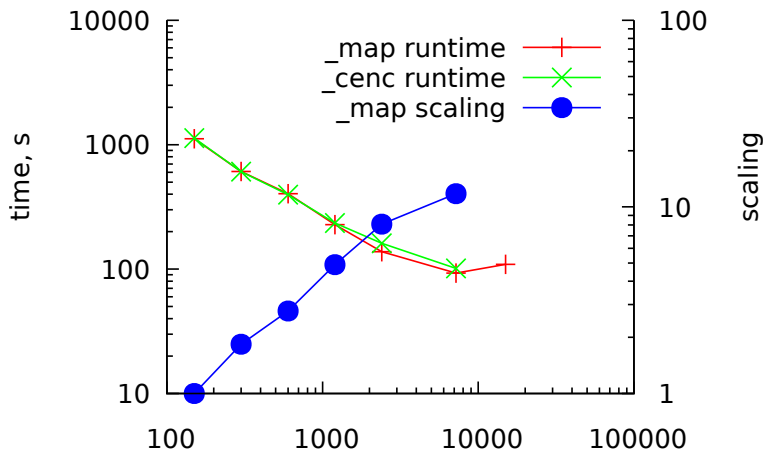
31.4%	3,110.7	589.3	15.9%	cgca_clvgp\$cgca_m3clvg_	
3.5%	346.0	513.0	59.7%	cgca_hxi\$cgca_m2hx_	
3.5%	342.0	175.0	33.8%	cgca_clvgn\$cgca_m3clvg_	
1.2%	116.3	4.7	3.9%	cgca_pfem_map\$cgca_m3pfem_	
1.1%	106.8	1,537.2	93.5%	cgca_clvgsd\$cgca_m3clvg_	
1.0%	99.9	24.1	19.5%	cgca_sld\$cgca_m3sld_	
=====					
38.4%	3,803.6	--	--	MPI	

14.6%	1,446.6	350.4	19.5%	mpi_bcast	
9.4%	932.4	473.6	33.7%	MPI_BARRIER	
7.0%	689.5	371.5	35.0%	mpi_recv	
4.9%	489.3	76.7	13.6%	MPI_ALLREDUCE	
1.5%	145.4	314.6	68.4%	MPI_REDUCE	
=====					
17.8%	1,766.8	--	--	ETC	

9.9%	983.9	8.1	0.8%	__DEALLOCATE	
6.6%	652.3	93.7	12.6%	gotoblas_dgemv_n_sandybridge	
=====					

Raw profiling data for ParaFEM/CG-PACK MPI/coarray miniapp with cgca_gcupdn and cgca_pfem_map at 7200 cores.

Profiling with cgca_pfem_map



Runtimes and scaling for ParaFEM/CGPACK MPI/coarray miniapp with `cgca_pfem_map` and `cgca_pfem_cenc`.

`cgca_pfem_map` or `cgca_pfem_cenc` are called only once during the execution of the miniapp. Hence only a minor improvement is obtained, only from about 1000 cores.

- [1] A. Shterenlikht, L. Margetts, and L. Cebamanos. Multi-scale CAFE framework for simulating fracture in heterogeneous materials implemented in fortran coarrays and mpi. In *PGAS Application Workshop (PAW), held in conjunction with SC16, Salt Lake City, UT, USA, 2016*. DOI: 10.1109/PAW.2016.006.
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- [3] A. Shterenlikht, L. Margetts, L. Cebamanos, and D. Henty. Fortran 2008 coarrays. *ACM Fortran Forum*, 34:10–30, 2015.
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- [7] A. Shterenlikht, S. Margetts, L. McDonald, and N. K. Bourne. Towards mechanism-based simulation of impact damage using exascale computing. In *Proc. 19th APS Conf. Shock Compression Condensed Matter SCCM-2015, JUN-2015, Tampa, Florida, USA, 2015*.
- [8] B. Long. Additional parallel features in Fortran. *ACM Fortran Forum*, 35:16–23, 2016.
- [9] C. A. Gandin and M. Rappaz. A coupled finite element-cellular automaton model for the prediction of dendritic grain structures in solidification processes. *Acta Met. and Mat.*, 42(7):2233–2246, 1994.

- [10] C. Zheng and D. Raabe. Interaction between recrystallization and phase transformation during intercritical annealing in a cold-rolled dual-phase steel: A cellular automaton model. *Acta Materialia*, 61:5504–5517, 2013.
- [11] A. Shterenlikht and I. C. Howard. The CAFE model of fracture – application to a TMCR steel. *Fatigue Fract. Eng. Mater. Struct.*, 29:770–787, 2006.
- [12] S. Das, A. Shterenlikht, I. C. Howard, and E. J. Palmiere. A general method for coupling microstructural response with structural performance. *Proc. Roy. Soc. A*, 462:2085–2096, 2006.